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# $\lambda$ -Calculus with Lazy Lists : Extended abstract (Algorithms in Algebraic Systems and Computation Theory)

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# $\lambda$ -Calculus with Lazy Lists

## – Extended Abstract –

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### Abstract

Into  $\lambda$ -calculus we introduce lazy lists  $\vec{a}$  whose naïve meaning is an infinite list consisting of variables,  $(a_0, a_1, a_2, \dots)$ . It is shown that there exist maps which form a Galois connection from Parigot's  $\lambda\mu$ -calculus to the  $\lambda$ -calculus with lazy list. The translations form not only an equational correspondence but also a reduction correspondence between the two calculi.

## 1 Introduction

We introduce lazy lists into  $\lambda$ -calculus. The introduction of infinite lists is motivated by a study on denotational semantics of type-free  $\lambda\mu$ -calculus [Pari92, Pari97, BHF99, BHF01].

Given domains  $U \times U \cong U \cong [U \rightarrow U]$  such as in Lambek-Scott [LS86], we have established a continuation denotational semantics of type-free  $\lambda\mu$ -calculus [Fuji02], which formally coincides with the CPS-translation [HS97, SR98, Fuji01] followed by the direct denotational semantics of the  $\lambda$ -calculus [Scot72, Stoy77]. See also the literature [HS97, SR98, Seli01] for continuation semantics of  $\lambda\mu$ -calculus.

This article shows that there exists a one-to-one correspondence between the  $\lambda\mu$ -calculus and the  $\lambda$ -calculus with lazy lists.

## 2 $\vec{\lambda}$ -calculus

We have two kinds of variables, the traditional variables in the  $\lambda$ -calculus denoted by  $x$  and variables for lazy lists denoted by  $\vec{a}$ . Our intended meaning is that  $\vec{a}$  denotes an infinite list of variables,  $\vec{a} \simeq (a_0, a_1, a_2, \dots)$ . The denotational meaning of  $\vec{a}$  would be given by elements of domain  $E^\omega$  which is a solution of the domain equation  $D \cong D \times D$ . From this intension, the expression  $M\vec{a}$  says that  $M$  is a function which can accept infinite inputs, and  $\lambda\vec{a}.M$  is a function characterized by  $D^D \cong D^{D \times D} \cong D^{D^D}$ , that is,  $\lambda\vec{a} \dots M\vec{a} \dots$  can behave like  $\lambda x \lambda\vec{a} \dots Mx\vec{a} \dots$ . Under this informal meaning, potentially infinite applications of  $\beta$ -reduction should be performed as follows:

$$\begin{aligned}
& (\lambda \vec{a}. \dots (M_1 \vec{a}) \dots) M \\
& \simeq (\lambda a_0 a_1 \dots \dots (M_1 a_0 a_1 \dots) \dots) M \\
& =_{\beta} \lambda a_1 a_2 \dots \dots (M_1 M a_1 a_2 \dots) \dots \\
& \simeq \lambda \vec{a}. \dots (M_1 M \vec{a}) \dots
\end{aligned}$$

Following this intended meaning, we define the  $\lambda$ -calculus with infinite lists as follows. A term in the form of  $\vec{a}$  is called a lazy list.

**Definition 1** ( $\vec{\lambda}$ -calculus)

$$\vec{\Lambda} \ni M ::= x \mid \vec{a} \mid \lambda x. M \mid \lambda \vec{a}. M \mid MM$$

$$(\beta) (\lambda x. M_1) M_2 = M_1[x := M_2]$$

$$(\eta) \lambda x. Mx = M \text{ if } x \notin FV(M)$$

$$(\vec{\beta}) (\lambda \vec{a}. M_1) M_2 = \begin{cases} M_1[\vec{a} := M_2] & \text{if } M_2 \text{ is in the form of a lazy list} \\ \lambda \vec{a}. M_1[\vec{a} := M_2] & \text{otherwise} \end{cases}$$

$$(\vec{\eta}) \lambda \vec{a}. M\vec{a} = M \text{ if } \vec{a} \notin FV(M)$$

The term  $M_1[x := M_2]$  denotes the usual capture-free substitution of  $M_2$  for  $x$  in  $M_1$ . The term  $M_1[\vec{a} := M_2]$  indicates the capture-free substitution defined in the following:

$$(i) x[\vec{a} := M] = x$$

$$(ii) \vec{b}[\vec{a} := M] = \begin{cases} M & \text{if } \vec{b} \equiv \vec{a} \text{ and } M \text{ is a lazy list} \\ M\vec{b} & \text{if } \vec{b} \equiv \vec{a} \text{ and } M \text{ is not a lazy list} \\ \vec{b} & \text{otherwise} \end{cases}$$

$$(iii) (\lambda x. M_1)[\vec{a} := M] = \lambda x. M_1[\vec{a} := M]$$

$$(iv) (\lambda \vec{b}. M_1)[\vec{a} := M] = \lambda \vec{b}. M_1[\vec{a} := M]$$

$$(v) (M_1 M_2)[\vec{a} := M] = \begin{cases} ((M_1[\vec{a} := M])M)M_2 & \text{if } M_2 \equiv \vec{a} \text{ and } M \text{ is not a lazy list} \\ (M_1[\vec{a} := M])(M_2[\vec{a} := M]) & \text{otherwise} \end{cases}$$

The axiom  $(\vec{\beta})$  says that a function which can accept an infinite list has taken an infinite list in the case where  $M_2$  is in the form of a lazy list. In the case where  $M_2$  is not in the form of a lazy list,  $(\vec{\beta})$  means that a function which can accept an infinite list has taken only a finite input, so that we still have  $\lambda \vec{a}$  even after this.  $(\vec{\eta})$  says that  $\lambda \vec{a}. M\vec{a}$  is an infinite  $\eta$ -expansion of  $M$ .

We write  $\vec{\Lambda} \vdash M_1 = M_2$  or  $(\beta, \eta, \vec{\beta}, \vec{\eta}) \vdash M_1 = M_2$  if  $M_1 = M_2$  is derived from the axioms  $(\beta)$ ,  $(\eta)$ ,  $(\vec{\beta})$ , or  $(\vec{\eta})$ . As an abbreviation, we may write  $M_1 =_{\vec{\Lambda}} M_2$  for this. We adopt a rewriting theory of  $\vec{\Lambda}$  by rewriting the left-hand side of each axiom to the corresponding right-hand side. The binary relation  $\rightarrow$ ,  $\rightarrow^+$ , or  $\rightarrow^*$  denotes the one-step rewriting, the transitive closure of  $\rightarrow$ , or the reflexive and transitive closure of  $\rightarrow$ , respectively.

**Proposition 1** (1)  $\vec{\Lambda} \vdash \lambda x. x = \lambda \vec{a}. \vec{a}$

$$(2) \vec{\Lambda} \vdash \lambda x. \lambda \vec{a}. M[\vec{a} := x] = \lambda \vec{a}. M$$

*Proof.* (1)  $\lambda \vec{a}. \vec{a}$  can be regarded as an infinite  $\eta$ -expansions of  $\lambda x. x$ :

$$\lambda \vec{a}. \vec{a} =_{\eta} \lambda x. (\lambda \vec{a}. \vec{a})x =_{\beta} \lambda x. (\lambda \vec{a}. x\vec{a}) =_{\eta} \lambda x. x$$

(2) The abstraction by  $\lambda x$  can be absorbed in the infinite  $\lambda$ -abstraction by  $\lambda \vec{a}$ :

Let  $x \notin FV(M)$ .

$$\lambda \vec{a}. M =_{\eta} \lambda x. (\lambda \vec{a}. M)x =_{\beta} \lambda x. \lambda \vec{a}. M[\vec{a} := x]$$

□

### 3 Relationship between $\lambda\mu$ -calculus and $\vec{\lambda}$ -calculus

We show that the  $\vec{\lambda}$ -calculus is a conservative extension over Parigot's  $\lambda\mu$ -calculus [Pari92, Pari97].

**Definition 2** ( $\lambda\mu$ -calculus)

$$\Lambda\mu \ni M ::= x \mid \lambda x. M \mid MM \mid \mu\alpha. M \mid [\alpha]M$$

$$(\beta) (\lambda x. M_1)M_2 = M_1[x := M_2]$$

$$(\eta) \lambda x. Mx = M \text{ if } x \notin FV(M)$$

$$(\mu) (\mu\alpha. M_1)M_2 = \mu\alpha. M_1[\alpha \Leftarrow M_2]$$

$$(\mu\beta) [\alpha](\mu\beta. M) = M[\beta := \alpha]$$

$$(\mu\eta) \mu\alpha. [\alpha]M = M \text{ if } \alpha \notin FV(M)$$

The  $\lambda\mu$ -term  $M_1[\alpha \Leftarrow M_2]$  denotes a term obtained by replacing each subterm of the form  $[\alpha]M$  in  $M_1$  with  $[\alpha](MM_2)$ . This operation is inductively defined as follows:

$$1. x[\alpha \Leftarrow M] = x$$

$$2. (\lambda x. M_1)[\alpha \Leftarrow M] = \lambda x. M_1[\alpha \Leftarrow M]$$

$$3. (M_1M_2)[\alpha \Leftarrow M] = (M_1[\alpha \Leftarrow M])(M_2[\alpha \Leftarrow M])$$

$$4. (\mu\beta. N)[\alpha \Leftarrow M] = \mu\beta. N[\alpha \Leftarrow M]$$

$$5. ([\beta]M_1)[\alpha \Leftarrow M] = \begin{cases} [\beta]((M_1[\alpha \Leftarrow M])M), & \text{for } \alpha \equiv \beta \\ [\beta](M_1[\alpha \Leftarrow M]), & \text{otherwise} \end{cases}$$

**Definition 3** Translation  $\lceil \cdot \rceil : \Lambda\mu \rightarrow \vec{\Lambda}$

$$1. \lceil x \rceil = x$$

$$2. \lceil \lambda x. M \rceil = \lambda x. \lceil M \rceil$$

$$3. \lceil M_1M_2 \rceil = \lceil M_1 \rceil \lceil M_2 \rceil$$

$$4. \lceil \mu\alpha.M \rceil = \lambda\vec{\alpha}.\lceil M \rceil$$

$$5. \lceil [\alpha]M \rceil = \lceil M \rceil \vec{\alpha}$$

**Lemma 1** Let  $M, N \in \Lambda\mu$ .

$$\lceil M[\alpha \leftarrow N] \rceil = \lceil M \rceil [\vec{\alpha} := \lceil N \rceil]$$

*Proof.* By induction on the structure of  $M$ . Noted that  $\lceil N \rceil$  cannot be a lazy list.  $\square$

**Proposition 2** If  $M_1 \rightarrow_{\Lambda\mu} M_2$ , then  $\lceil M_1 \rceil \rightarrow_{\vec{\Lambda}} \lceil M_2 \rceil$ .

*Proof.* By induction on the derivation of  $M_1 \rightarrow_{\Lambda\mu} M_2$ . We show some of the base cases.

Case of  $(\mu)$ :

$$\begin{aligned} \lceil (\mu\alpha.M)N \rceil &= (\lambda\vec{\alpha}.\lceil M \rceil) \lceil N \rceil \\ &\rightarrow_{\beta} \lambda\vec{\alpha}.\lceil M \rceil [\vec{\alpha} := \lceil N \rceil] \text{ since } \lceil N \rceil \text{ is not a lazy list} \\ &= \lambda\vec{\alpha}.\lceil M[\alpha \leftarrow N] \rceil = \lceil \mu\alpha.M[\alpha \leftarrow N] \rceil \end{aligned}$$

Case of  $(\beta)$ :

$$\begin{aligned} \lceil (\lambda x.M)N \rceil &= (\lambda x.\lceil M \rceil) \lceil N \rceil \\ &\rightarrow_{\beta} \lceil M \rceil [x := \lceil N \rceil] = \lceil M[x := N] \rceil \end{aligned}$$

$\square$

**Definition 4** Translation  $\lfloor \cdot \rfloor : \vec{\Lambda} \rightarrow \Lambda\mu$

$$(i) \lfloor x \rfloor = x$$

$$(ii) \lfloor \vec{a} \rfloor = [a](\lambda x.x)$$

$$(iii) \lfloor \lambda x.M \rfloor = \lambda x.\lfloor M \rfloor$$

$$(iv) \lfloor \lambda \vec{a}.M \rfloor = \mu a.\lfloor M \rfloor$$

$$(v) \lfloor M_1 M_2 \rfloor = \begin{cases} [a]\lfloor M_1 \rfloor & \text{if } M_2 \equiv \vec{a} \text{ for some } \vec{a} \\ \lfloor M_1 \rfloor \lfloor M_2 \rfloor & \text{otherwise} \end{cases}$$

**Lemma 2** (i) Let  $M \in \vec{\Lambda}$ .

$$\lfloor M \rfloor [a := b] = \lfloor M[\vec{a} := \vec{b}] \rfloor$$

(ii) Let  $M, N \in \vec{\Lambda}$  where  $N$  is not a lazy list.

$$\lfloor M \rfloor [a \leftarrow \lfloor N \rfloor] \rightarrow_{\beta}^* \lfloor M[\vec{a} := N] \rfloor$$

*Proof.* By induction on the structure of  $M$ . We show some cases for (ii).

Case of  $M \equiv \vec{a}$ :

$$\begin{aligned} \lfloor \vec{a} \rfloor [a \leftarrow \lfloor N \rfloor] &= ([a](\lambda x.x)) [a \leftarrow \lfloor N \rfloor] = [a]((\lambda x.x) \lfloor N \rfloor) \\ &\rightarrow_{\beta} [a] \lfloor N \rfloor = \lfloor N \vec{a} \rfloor = \lfloor \vec{a}[\vec{a} := N] \rfloor \text{ since } N \text{ is not a lazy list.} \end{aligned}$$

Case of  $M \equiv M_1 M_2$ :

We show the subcase  $M_2$  of  $\vec{a}$  here.

$$\lfloor M_1 M_2 \rfloor [a \leftarrow \lfloor N \rfloor] = \lfloor M_1 \vec{a} \rfloor [a \leftarrow \lfloor N \rfloor]$$

$$\begin{aligned}
&= ([a][M_1])[a \leftarrow [N]] \\
&= [a]([M_1][a \leftarrow [N]])[N] \\
&\rightarrow_{\beta}^* [a]([M_1[\vec{a} := N]])[N] \quad \text{by the induction hypothesis} \\
&= [a]([M_1[\vec{a} := N]N]) \\
&= [(M_1[\vec{a} := N]N)\vec{a}] = [(M_1\vec{a})[\vec{a} := N]]
\end{aligned}$$

□

**Proposition 3** *Let  $M_1, M_2 \in \vec{\Lambda}$ .*

*If  $M_1 \rightarrow_{\vec{\Lambda}} M_2$  then  $[M_1] \rightarrow_{\Lambda\mu}^+ [M_2]$ .*

*Proof.* By induction on the derivation of  $M_1 \rightarrow_{\vec{\Lambda}} M_2$ .

Case of  $(\vec{\beta})$  where  $N$  is not a lazy list:

$$\begin{aligned}
&[(\lambda\vec{a}.M)N] = (\mu a.[M])[N] \\
&\rightarrow_{\mu} \mu a.[M][a \leftarrow [N]] \\
&\rightarrow_{\beta}^* \mu a.[M[\vec{a} := N]] \quad \text{by Lemma 2} \\
&= [\lambda\vec{a}.M[\vec{a} := N]]
\end{aligned}$$

Case of  $(\vec{\beta})$  where  $N$  is a lazy list:

$$\begin{aligned}
&[(\lambda\vec{a}.M)\vec{b}] = [b](\mu a.[M]) \\
&\rightarrow_{\mu\beta} [M][a := b] = [M[\vec{a} := \vec{b}]]
\end{aligned}$$

Case of  $(\beta)$ :

$$\begin{aligned}
&[(\lambda x.M)N] = (\lambda x.[M])[N] \\
&\rightarrow_{\beta} [M][x := [N]] = [M[x := N]] \quad \text{by Lemma 2}
\end{aligned}$$

□

**Proposition 4** *The maps  $\lceil \cdot \rceil : \Lambda\mu \rightarrow \vec{\Lambda}$  and  $\lfloor \cdot \rfloor : \vec{\Lambda} \rightarrow \Lambda\mu$  establish a one-to-one correspondence between  $\Lambda\mu$  and  $\vec{\Lambda}$ :*

(i) *For any  $M \in \Lambda\mu$ ,  $M = \lfloor \lceil M \rceil \rfloor$ .*

(ii) *For any  $M \in \vec{\Lambda}$ ,  $\lceil \lfloor M \rfloor \rceil \rightarrow_{\beta}^* M$ .*

*Proof.* By induction on the structure of  $M$ . For (ii) we show one of the base cases.

Case of  $M \equiv \vec{a}$ :

$$\lceil [\vec{a}] \rceil = \lceil [a](\lambda x.x) \rceil = (\lambda x.x)\vec{a} \rightarrow_{\beta} \vec{a}$$

□

**Definition 5 (Sabry-Walder [SW96])**

*The maps  $\lceil \cdot \rceil$  and  $\lfloor \cdot \rfloor$  form a Galois connection from  $\Lambda\mu$  to  $\vec{\Lambda}$  whenever  $M \rightarrow_{\Lambda\mu}^* [P]$  if and only if  $\lceil M \rceil \rightarrow_{\vec{\Lambda}}^* P$ .*

$$\begin{array}{ccc}
M \in \Lambda\mu & \xrightarrow{\lceil \cdot \rceil} & \vec{\Lambda} \ni \lceil M \rceil \\
\downarrow \text{\scriptsize $*\downarrow_{\Lambda\mu}$} & & \downarrow \text{\scriptsize $*\downarrow_{\vec{\Lambda}}$} \\
[P] \in \Lambda\mu & \xleftarrow{\lfloor \cdot \rfloor} & \vec{\Lambda} \ni P
\end{array}$$

It can be confirmed that the maps  $\lceil \cdot \rceil : \Lambda\mu \rightarrow \vec{\Lambda}$  and  $\lfloor \cdot \rfloor : \vec{\Lambda} \rightarrow \Lambda\mu$  form a Galois connection by Propositions 2, 3, 4, and the following proposition:

**Proposition 5 (Sabry-Wadler [SW96])**

The maps  $\lceil \cdot \rceil$  and  $\lfloor \cdot \rfloor$  form a Galois connection from  $\Lambda\mu$  to  $\vec{\Lambda}$  if and only if conditions hold:

- (i)  $M \rightarrow_{\Lambda\mu}^* \lfloor \lceil M \rceil \rfloor$ ,
- (ii)  $\lceil \lfloor P \rfloor \rceil \rightarrow_{\vec{\Lambda}}^* P$ ,
- (iii)  $M_1 \rightarrow_{\Lambda\mu}^* M_2$  implies  $\lceil M_1 \rceil \rightarrow_{\vec{\Lambda}}^* \lceil M_2 \rceil$ , and
- (iv)  $P_1 \rightarrow_{\vec{\Lambda}}^* P_2$  implies  $\lfloor P_1 \rfloor \rightarrow_{\Lambda\mu}^* \lfloor P_2 \rfloor$ .

See also the following diagrams:

$$\begin{array}{ll}
 \text{(i)} & \begin{array}{ccc} M \in \Lambda\mu & \xrightarrow{\lceil \cdot \rceil} & \vec{\Lambda} \ni \lceil M \rceil \\ \downarrow *_{\Lambda\mu} & & \parallel \\ \lfloor \lceil M \rceil \rfloor \in \Lambda\mu & \xleftarrow{\lfloor \cdot \rfloor} & \vec{\Lambda} \ni \lfloor \lceil M \rceil \rfloor \end{array} \\
 \text{(ii)} & \begin{array}{ccc} \lceil P \rceil \in \Lambda\mu & \xrightarrow{\lceil \cdot \rceil} & \vec{\Lambda} \ni \lceil \lfloor P \rfloor \rceil \\ \parallel & & \downarrow *_{\vec{\Lambda}} \\ \lfloor P \rfloor \in \Lambda\mu & \xleftarrow{\lfloor \cdot \rfloor} & \vec{\Lambda} \ni P \end{array} \\
 \text{(iii)} & \begin{array}{ccc} M_1 \in \Lambda\mu & \xrightarrow{\lceil \cdot \rceil} & \vec{\Lambda} \ni \lceil M_1 \rceil \\ \downarrow *_{\Lambda\mu} & & \downarrow *_{\vec{\Lambda}} \\ M_2 \in \Lambda\mu & \xrightarrow{\lceil \cdot \rceil} & \vec{\Lambda} \ni \lceil M_2 \rceil \end{array} \\
 \text{(iv)} & \begin{array}{ccc} \lfloor P_1 \rfloor \in \Lambda\mu & \xleftarrow{\lfloor \cdot \rfloor} & \vec{\Lambda} \ni P_1 \\ \downarrow *_{\Lambda\mu} & & \downarrow *_{\vec{\Lambda}} \\ \lfloor P_2 \rfloor \in \Lambda\mu & \xleftarrow{\lfloor \cdot \rfloor} & \vec{\Lambda} \ni P_2 \end{array}
 \end{array}$$

**Proposition 6 (i) (Conservative extension)** *Let  $M_1, M_2 \in \Lambda\mu$ .*

*If we have  $\lceil M_1 \rceil =_{\vec{\Lambda}} \lceil M_2 \rceil$ , then  $M_1 =_{\Lambda\mu} M_2$ .*

**(ii) (Galois connection)**

*The maps  $\lceil \cdot \rceil : \Lambda\mu \rightarrow \vec{\Lambda}$  and  $\lfloor \cdot \rfloor : \vec{\Lambda} \rightarrow \Lambda\mu$  form a Galois connection from  $\lambda\mu$ -calculus to the  $\vec{\lambda}$ -calculus.*

(iii) (Equational/reduction correspondence)

(1)  $M_1 =_{\Lambda\mu} M_2$  if and only if  $\lceil M_1 \rceil =_{\bar{\Lambda}} \lceil M_2 \rceil$ .

In particular,  $M_1 \rightarrow_{\Lambda\mu}^+ M_2$  if and only if  $\lceil M_1 \rceil \rightarrow_{\bar{\Lambda}}^+ \lceil M_2 \rceil$ .

(2)  $P_1 =_{\bar{\Lambda}} P_2$  if and only if  $\lfloor P_1 \rfloor =_{\Lambda\mu} \lfloor P_2 \rfloor$ .

*Proof.* (i) From Proposition 4.

(ii) From Propositions 2, 3, 4, and 5.

(iii) From (ii). □

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